

## Introduction to Vectors (6.1)

### Math Learning Target:



"I know what a scalar and vector quantity is, and I cite several examples. I know some fundamental properties of vectors. I can describe and represent geometric vectors."

A **scalar quantity** is a physical quantity that can be described by one real number, often accompanied by units of measurement. This real number is the scalar's size or **magnitude**.

Examples: temperature ( $-10^{\circ}\text{C}$ )  
internet download speed (100mb/s)

A **vector quantity** is a physical quantity that has both magnitude and direction. Vectors are drawn as arrows.

Examples: change in temp ( $-2^{\circ}\text{C}$  OR  $2^{\circ}\text{C}$  [down])  
force (2N [right])

The diagram shows a blue arrow pointing to the right. The left end is labeled 'tail' and the right end is labeled 'head'. A bracket above the arrow is labeled 'magnitude'. A bracket below the arrow is labeled 'direction'. To the right of the arrow, the text 'Notation:  $\vec{AB}$  OR  $\overrightarrow{AB}$ ' is written.

A vector's magnitude is always non-negative. If it is not a vector, it may be any real number.

A **geometric vector** is a vector without regard to a coordinate system.

### Common Examples of Scalar and Vector Quantities

#### Scalar

**Distance:** the length between two positions of an object.

**Speed:** the rate of change of distance, per unit of time.

**Mass:** the amount of matter contained within an object.

#### Vector

**Position:** the distance and direction of an object, relative to a point of reference.

**Displacement:** the change in position of an object, in a given direction.

**Velocity:** the rate of change in position of an object, per unit of time, in a given direction. Thus, it is the rate of displacement per unit of time, in a given direction.

**Acceleration:** the rate of change of velocity, per unit of time, in a given direction.

**Weight:** the resultant (net) force of gravity on an object, in a given direction.

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mass  $\neq$  weight

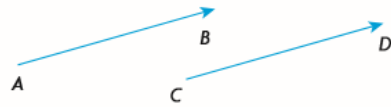
### Opposite Vectors

Two vectors that are opposites have the same magnitude but point in opposite directions.



$\vec{AB}$  and  $\vec{BA}$  are opposites, and  $\vec{AB} = -\vec{BA}$ . In this case,  $|\vec{AB}| = |\vec{BA}|$  and the vectors are parallel but point in opposite directions. Vectors can also be represented with lower-case letters. In the diagram above, vectors  $\vec{v}$  and  $-\vec{v}$  have the same magnitude, i.e.,  $|\vec{v}| = |-\vec{v}|$ , but point in opposite directions, so  $\vec{v}$  and  $-\vec{v}$  are also opposites.

### Equal Vectors



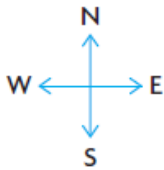
Two vectors  $\vec{AB}$  and  $\vec{CD}$  are equal (or equivalent) if and only if

1.  $\vec{AB}$  and  $\vec{CD}$  are parallel to each other, and the direction from A to B is the same as the direction from C to D
2. the magnitude of  $\vec{AB}$  equals the magnitude of  $\vec{CD}$ , i.e.,  $|\vec{AB}| = |\vec{CD}|$

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When drawing a vector, its length is always proportional to its magnitude.

**Example** A car is travelling East at 80 km/h. Draw this vector using the scale 1 cm: 10 km/h



<https://youtu.be/LWGJA9i18Co> <<<<< How can the Force of gravity be  $\vec{0}$  on Earth? Huh?

### ***MathSIP!***

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\*In 6e, change "east" to "south".